#lab 7 Gauss method :

import numpy as np

import sys

# Reading number of unknowns

n = int(input('Enter number of unknowns: ')) # its saves the shape of matrix

# Making numpy array of n x n+1 size and initializing

# to zero for storing augmented matrix

a = np.zeros((n,n+1)) # its forms the a[][]

# Making numpy array of n size and initializing

# to zero for storing solution vector

x = np.zeros(n) # it assign the argument of x with 0

# Reading augmented matrix coefficients

print('Enter Augmented Matrix Coefficients:') #its reads actual matrix value

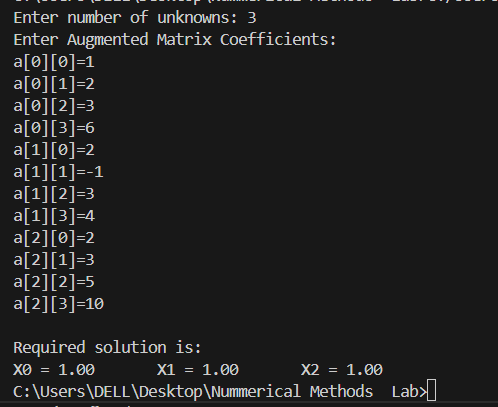
for i in range(n): # loop for running upto n -1 if the users ip shape 3 goes to goes to 0 to 2

    for j in range(n+1):

        a[i][j] = float(input( 'a['+str(i)+']['+ str(j)+']='))

# Applying Gauss Elimination

for i in range(n):

    if a[i][i] == 0.0:

        sys.exit('Divide by zero detected!')

    for j in range(i+1, n):

        ratio = a[j][i]/a[i][i]

        for k in range(n+1):

            a[j][k] = a[j][k] - ratio \* a[i][k]

# Back Substitution

x[n-1] = a[n-1][n]/a[n-1][n-1]

for i in range(n-2,-1,-1):

    x[i] = a[i][n]

    for j in range(i+1,n):

        x[i] = x[i] - a[i][j]\*x[j]

    x[i] = x[i]/a[i][i]

# Displaying solution

print('\nRequired solution is: ')

for i in range(n):

    print('X%d = %0.2f' %(i,x[i]), end = '\t')

    Lab 8:  
#Power Method

# Power Method to Find Largest Eigen Value and Eigen Vector

# Importing NumPy Library

import numpy as np

import sys

# Reading order of matrix

n = int(input('Enter order of matrix: '))

# Making numpy array of n x n size and initializing

# to zero for storing matrix

a = np.zeros((n,n))

# Reading matrix

print('Enter Matrix Coefficients:')

for i in range(n):

    for j in range(n):

        a[i][j] = float(input( 'a['+str(i)+']['+ str(j)+']='))

# Making numpy array n x 1 size and initializing to zero

# for storing initial guess vector

x = np.zeros((n))

# Reading initial guess vector

print('Enter initial guess vector: ')

for i in range(n):

    x[i] = float(input( 'x['+str(i)+']='))

# Reading tolerable error

tolerable\_error = float(input('Enter tolerable error: '))

# Reading maximum number of steps

max\_iteration = int(input('Enter maximum number of steps: '))

# Power Method Implementation

lambda\_old = 1.0

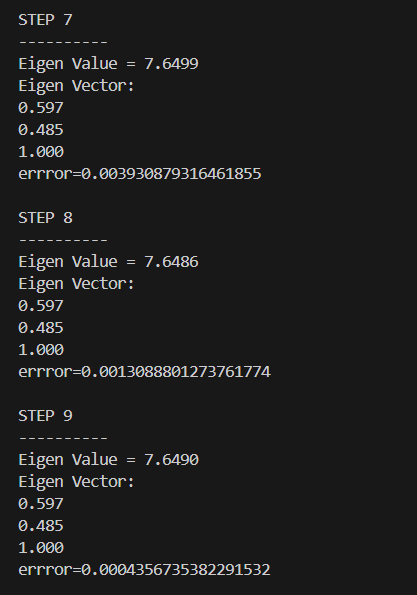
condition =  True

step = 1

while condition:

    # Multiplying a and x

    x = np.matmul(a,x)

    # Finding new Eigen value and Eigen vector

    lambda\_new = max(abs(x))

    x = x/lambda\_new

    # Displaying Eigen value and Eigen Vector

    print('\nSTEP %d' %(step))

    print('----------')

    print('Eigen Value = %0.4f' %(lambda\_new))

    print('Eigen Vector: ')

    for i in range(n):

        print('%0.3f\t' % (x[i]))

    # Checking maximum iteration

    step = step + 1

    if step > max\_iteration:

        print('Not convergent in given maximum iteration!')

        break

    # Calculating error

    error = abs(lambda\_new - lambda\_old)

    print('errror='+ str(error))

    lambda\_old = lambda\_new

    condition = error > tolerable\_error

**Discussion and Conclusion**:

The Gauss elimination method systematically reduces a system of linear equations to an upper triangular form, making it efficient for direct solutions, especially for small to medium-sized systems. It ensures accuracy but can become unstable with ill-conditioned matrices unless partial pivoting is used. On the other hand, the Power method is an iterative technique specifically designed to find the dominant eigenvalue and its corresponding eigenvector of a matrix. It is simple to implement and works well when the dominant eigenvalue is significantly larger than the others. However, it may fail or converge slowly if this condition is not met. Both methods highlight the balance between direct and iterative strategies in numerical methods—Gauss focusing on precision and generality, while Power emphasizes simplicity and specific applications in eigenvalue problems.